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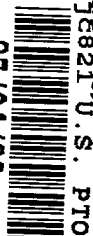
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PATENT APPLICATION

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Sir:

Transmitted herewith for filing is the patent application of Inventor(s):

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Pietro Buttolo

For: **METHOD FOR RECONSTRUCTING THE TOPOGRAPHICAL INFORMATION OF A POLYGONAL SOUP**

Enclosed are:

- ☒ 5 sheet(s) of drawings
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METHOD FOR RECONSTRUCTING THE TOPOLOGY OF A POLYGONAL SOUP

Technical Field

The present invention relates to
5 visualization tools for interactive simulations with
complex vehicle models.

Background Of The Invention

To meet the need for interactive simulations
with complex vehicle models, a generation of
10 visualization tools have been developed. However, most
of these tools have limitations inherent in their data
structure. In this regard, most visualization tools
have adopted a polygonal soup, that is, an unstructured
collection of polygons, as their standard data
15 representation. However, a variety of existing
applications, such as CFD (Computational Fluid
Dynamics), FEA (Finite Element Analysis), and assembly
simulation, require more than a cloud of points or
triangles.

20 Thus, a need exists for a method of
reconstructing the topographical information
(relationships between polygons) of a polygonal soup in
order to overcome the known problems with visualization
tools.

Summary of the Invention

25 The object of the present invention is to
provide an improved visualization tool for interactive

simulation with complex vehicle models. It is another object of the present invention to provide a visualization tool that comprises more than a cloud of points or triangles.

5 - In accordance with the present invention, an algorithm is provided which automatically reconstructs topological information for a given mesh and then alters the mesh by introducing, deleting, or splitting existing polygons when needed.

10 In accordance with the present invention, a new OctTree space decomposition is used to achieve a log2-complexity search which locates the closest vertex in the polygonal soup to a given point in space. A technique with linear complexity is then used to locate
15 all of the triangles connected to that vertex. A technique with linear complexity is also used to find all triangles connected to a given triangle. The triangles are then split to enforce conductivity.

20 These and other objects, features, and advantages of the present invention will become apparent from the following detailed description of the invention when viewed in accordance with the accompanying drawings and appended claims.

Brief Description Of The Drawings

25 FIGURE 1 depicts an exemplary cube representation for modeling tessellated meshes;

 FIGURE 2 sets forth index representations of the triangles and vertices of the cube depicted in Figure 1;

FIGURE 3 depicts a dynamic vector vertex-neighbor table;

FIGURE 4 depicts tables generated from the vertex-neighbor table;

5 - FIGURE 5 depicts a dynamic vector edge-neighbor table;

FIGURE 6 illustrates an object compound of unconnected strips of connected triangles;

FIGURE 7 depicts a generalized example of a
10 step in synchronizing triangle strips;

FIGURE 8 depicts the formation of new triangles;

FIGURE 9 illustrates the exemplary cube as modified;

15 FIGURE 10 illustrates another step in the sorting process;

FIGURE 11 illustrates another step in the sorting process;

FIGURE 12 depicts another sorting example;

20 FIGURE 13 depicts still another sorting example;

FIGURE 14 illustrates an OctTree example; and

FIGURE 15 depicts a further sorting example.

Description Of The Preferred Embodiment(s)

25 As indicated, there is a need for interactive simulation with complex systems, such as airplanes and cars, and in fact visualization tools have been developed which are capable of rendering large models in real-time. However, in developing the 3-D rendering

representation of Figure 2 is generated. An initial attempt of reducing duplicated vertices is performed at this stage. In this regard, the first step operation is only required when the geometry is described as an explicit set of triangles, such as STL. In the second and third steps, the vertex-neighbors, and edge-neighbor tables are developed.

The vertex-neighbors table is a dynamic vector where, for each vertex, the list of all the connected triangles is immediately available, as is shown in Figure 3. The algorithm sequentially browses the triangle list. For each triangle, the table listed in Figure 2 contains the indexes of the three vertices. An identifier, pointing to the triangle sequential number in the triangle-list is added to the index-neighbor list, in correspondence to each vertex. For example, in the case of the cube shown in Figure 1, this method would start by looking at the triangle T_0 with vertices V_0 , V_1 , and V_3 . Table A in Figure 4 is then generated.

Proceeding with T_1 , the additional entries are added to Table B. Thereafter, the complete vertex-neighbor Table C is developed. Since the triangle-index table is traversed only one time, this creates an efficient, linear-complexity algorithm. In this regard, the number of computations is $n_t \times 3$, where n_t is the number of triangles.

The edge-neighbors table is a vector of lists with an entry for each triangle. Each list has three elements, one for each edge of the given triangle, $V_{11}-V_{12}$, $V_{12}-V_{13}$, and $V_{13}-V_{10}$, respectively, depending on the

position of the element in the list. These elements can be equal to either -1, to represent an unconnected edge, or to the sequential number of the connected triangle to the selected edge, as can be seen in Figure 5. Thereafter, the algorithm sequentially browses the triangle list, starting with the first element, and determines if there are other triangles that share any of its three edges. For example, with the cube illustrated in Figure 1, the first edge V_0V_1 of the first triangle T_0 can be viewed as follows:

Triangle	V_{i1}	V_{i2}	V_{i3}
T_0	V_0	V_1	V_3
...

(1)

Two triangles are connected at an edge if they share the same two vertices making up the edge extremes, in this case V_0 and V_1 . Then, a list of potential candidates is found looking for all triangles connected to V_0 that are not T_0 in the vertex-neighbors table. This is shown as follows:

Vertex	T_{i1}	T_{i2}
V_0	T_0	T_8	T_9	T_{10}	T_{11}
...

(2)

Since there are now four triangles, T_8 - T_{11} , it is necessary to look at the triangle table to see if any of the candidates contains the vertex V_1 as well:

<i>Triangle</i>	V_{i1}	V_{i2}	V_{i3}
T_8	V_1	V_0	V_5
T_9	V_4	V_5	V_0
T_{10}	V_3	V_7	V_0
T_{11}	V_4	V_0	V_7

(3)

In this particular example, the first edges of T_0 and the first edge of T_8 share the same vertices V_1 and V_0 . The two triangles are connected, and the edge-neighbor table is then updated as shown below:

<i>Triangle</i>	T_{i1}	T_{i2}	T_{i3}
T_0	T_8		
...
T_8	T_0		
...

(4)

As a result, after browsing all of the edges of all of the triangles, the following table is completed:

<i>Triangle</i>	T_{i1}	T_{i2}	T_{i3}
T_0	T_8	T_1	T_{10}
T_1	T_2	T_0	T_4
T_2	T_4	T_3	T_1
T_3	T_{10}	T_2	T_7
T_4	T_1	T_5	T_2
T_5	T_7	T_4	T_8
T_6	T_{11}	T_7	T_9
T_7	T_5	T_6	T_3
T_8	T_0	T_9	T_5
T_9	T_6	T_8	T_{11}
T_{10}	T_3	T_{11}	T_0
T_{11}	T_9	T_{10}	T_6

(5)

As shown in Table (5), it is noted that there are not any unconnected edges and, therefore, this particular geometry is a manifold body.

The total number of computations depends on the average number of triangles connected to a given vertex. The triangle/vertex ratio $n_{t/v}$ ranges from a value of three in the case of a tetrahedron, to 4.5 for the cube described above, to about 5.0 for typical automotive models. This means that the number of computations to find the triangle connected to a given edge is:

$$(n_{t/v}-1) \cdot 3 \quad (6)$$

Since each triangle has three edges, and there are n_t triangles, then the total number of computations is:

$$n_t \cdot (n_{t/v}-1) \cdot 9 \approx n_t \cdot 36 \quad (7)$$

This provides an efficient, linear-complexity algorithm.

The algorithms used to reconstruct the topographical information of a tessellated mesh, as discussed above, rely on two assumptions. The first assumption is that duplicate vertices have the same coordinates. This requirement is a foundation of a variety of search engines, usually based on balanced trees or skip-lists, used to detect duplicate vertices. The second assumption is that the tessellation is built without gaps. This translates in having strips or fans of triangles all topologically connected at the same set of vertices. However, in particular with VRML and OpenGL files, the objects are composed of unconnected strips of connected triangles, as shown in Figure 6. This prevents building of edge connectivity since two triangles are considered connected at an edge only if they share the entire edge.

As a result, existing visualization tools for complex systems have a plurality of gaps, poor alignment, and degenerate meshes. Also, duplicate vertices and the synchronization of triangle strips are not sufficiently taken into account.

In the present invention, these problems with existing systems are considered and taken into account. Duplicate vertices are eliminated and triangle strips are synchronized. The algorithm for accomplishing this is described below.

If the vertex V_0 is duplicated and the copies replaced by the vertex V_{0b} in the cube model described

above to describe the triangles T_{10} and T_{11} , the new vertex and triangle list are then modified as follows:

5	Vertex	X	Y	Z	Triangle	V_{i1}	V_{i2}	V_{i3}	(8)
	V_0	-1	-1	+1	
	V_{0b}	-1	-1	+1	T_{10}	V_3	V_7	V_{0b}	
	T_{11}	V_4	V_{0b}	V_7	

10 Due to the new duplicate vertex, the vertex-neighbors and edge-neighbors tables are also changed to the following:

15	Vertex	T_{i1}	T_{i2}	Triangle	T_{i1}	T_{i2}	T_{i3}	(9)
	V_0	T_0	T_8	T_9			T_0	T_8	T_1	-1	
	V_{0b}	T_{10}	T_{11}				T_9	T_6	T_8	-1	
	T_{10}	T_3	T_{11}	-1	
							T_{11}	-1	T_{10}	T_6	

20 As a result, all four triangles, T_0 , T_9 , T_{10} , and T_{11} , now each have an unconnected edge.

In order to remove duplicate vertices, the algorithm first browses the edge table searching for
 25 unconnected edges. Once an edge is found, duplicate copies of either one of the two vertices at the ends of the segment are looked for, by searching in the vertex list for the closest vertex. In Table 8 above, vertices V_0 and V_{0b} have the same coordinates, and
 30 therefore have minimum distance, equal to zero. However, in other cases, the distance is small, but

significant. It is necessary to make sure that the mesh will not degenerate once a vertex is replaced with another one.

Once a duplicate vertex has been found, the procedure is as follows: (a) in the triangle index table, all references to the duplicate vertices are replaced with a reference to the original vertex; (b) the entry in the vertex table for the duplicate vertex is removed and the appropriate connected triangles are added to the entry list of the original vertex; and; and (c) the edge table for all triangles connected to "original" vertices are rebuilt. When applied to the copy of duplicated vertices, V_0 and V_{0b} , this sequence restores the original vertex, triangle, vertex-neighbors and edge-neighbors tables.

The problem with synchronizing triangle strips, such as those depicted in Figure 6, can be generalized as shown in Figure 7 as a vertex falling inside another triangle edge. The introduction of two new triangles, namely T_{1a} and T_{1b} as well as a new vertex V_8 , changes the vertex and triangle table as follows:

Vertex	Triangle		
	X	Y	Z
...
V_8	0	0	+1

Triangle	Vertex		
	V_{11}	V_{12}	V_{13}
...
T_{1a}	V_2	V_8	V_1
T_{1b}	V_2	V_3	V_8
...

(10)

As evident from the new edge-neighbor table, there are three edges that are not connected:

<i>Triangle</i>	T_{11}	T_{12}	T_{13}
T_0	T_8	-1	T_{10}
T_{1a}	T_{1b}	-1	T_4
T_{1b}	T_2	-1	T_{1a}
...

(11)

There are different alternatives for building a topological connection. First, an artificial vertex could be introduced in the triangle T_0 . However, this would require dealing with polygons having different numbers of sides since with a new vertex, T_0 , would be a quadrilateral. Secondly, the vertex V_8 could be moved to overlap either one of the two vertices V_1 or V_3 , and then be eliminated. However, this approach would only modify the geometry, with the potential loss of important details, if the triangles connected to V_8 do not share the same normal. Thirdly, the triangle T_0 could be split into two new triangles, replacing the edge V_1V_3 with V_1V_8 and V_3V_8 , respectively.

The present invention implements the latter alternative. As in the method dealing with duplicated edges, the algorithm browses the edge table looking for unconnected edges. Once an edge is found, it then looks for any vertex that falls very close to the edge itself, but not on one of its vertices. In the example shown in Figure 7, the first unconnected edge that is

<i>Triangle</i>	V_{i1}	V_{i2}	V_{i3}
T_0	V_0	$V_{1...}$	V_3
...

<i>Triangle</i>	T_{11}	T_{12}	T_{13}
T_0	T_8	-1	T_{10}
T_{1a}	T_{1b}	-1	T_4
T_{1b}	T_2	-1	T_{10}
...

(12)

encountered is the second edge V_1V_3 of the triangle T_0 :
 Searching in the vertex list, the closest vertex to
 this segment is V_8 . Since the distance to the segment
 is equal to zero, and the distance to both segment
 5 extremes is equal to $\sqrt{2}$, the vertex is recognized to
 fall on an inside edge. Once the closest vertex is
 found, it is necessary to search in the vertex-
 neighbors table to see if there is a triangle connected
 to it which has an unconnected edge parallel to the
 10 original edge. Moreover, the triangle must not overlap
 the original triangle. In the "cube" example discussed
 above, there are two triangles connected to V_8 :

Vertex	T_{i1}	T_{i2}
...	...				
V_8	T_{1a}	T_{1b}			

(13)

15 Once a triangle, edge, and vertex have been
 identified, the geometry is then re-meshed by splitting
 the triangle. First, the triangle table is updated to
 reflect the fact that the original triangle is split
 into two new elements. In general, the original
 20 triangle is kept with one of its vertex indexes
 replaced and a new triangle is added. The triangle
 table will then change as follows:

Triangle	V_{i1}	V_{i2}	V_{i3}
T_0	V_0	V_1	V_3
...

Triangle	V_{i1}	V_{i2}	V_{i3}
T_0	V_0	V_1	V_8
...
T_{12}	V_0	V_8	V_3

(14)

In the generic case, the algorithm must take into account which edge the unconnected vertex falls on, as shown in Figure 8. The generic rules to update the triangle table are then summarized as follows:

5

		Before			After		
Triangle		V _{i1}	V _{i2}	V _{i3}	V _{i1}	V _{i2}	V _{i3}
edge V _{i1} -V _{i2}	T _{orig}	V _{i1}	V _{i2}	V _{i3}	V _{i1}	V _{new}	V _{i3}
	T _{new}	--	--	--	V _{new}	V _{i2}	V _{i3}
edge V _{i2} -V _{i3}	T _{orig}	V _{i1}	V _{i2}	V _{i3}	V _{i1}	V _{i2}	V _{new}
	T _{new}	--	--	--	V _{i1}	V _{new}	V _{i3}
edge V _{i3} -V _{i1}	T _{orig}	V _{i1}	V _{i2}	V _{i3}	V _{new}	V _{i2}	V _{i3}
	T _{new}	--	--	--	V _{i1}	V _{i2}	V _{new}

(15)

10

Thereafter, the vertex-neighbor table is updated. In the case of the cube shown in Figure 7, this would change as follows:

20

Vertex	T _{i1}	T _{i2}
V ₀	T ₀	T ₈	T ₉	T ₁₀	T ₁₁
V ₁	T ₀	T _{1a}	T ₄	T ₅	T ₈
...		
V ₃	T ₀	T _{1b}	T ₂	T ₃	T ₁₀
...		
V ₈	T _{1a}	T _{1b}			

(16)

25

Vertex	T _{i1}	T _{i2}
V ₀	T ₀	T ₈	T ₉	T ₁₀	T ₁₁	T ₁₂
V ₁	T ₀	T _{1a}	T ₄	T ₅	T ₈	
...			
V ₃	T _{1b}	T ₂	T ₃	T ₁₀	T ₁₂	
...			
V ₈	T _{1a}	T _{1b}	T ₀	T ₁₂		

30

In the general case, the following table summarizes the rules needed for determining the new table, depending on which of the three angles is affected by the new vertex:

5		Before			After	
		Vertex	T_{i1}	...	T_{i1}	
10	edge	V_{i1}	
	$V_{i1}-V_{i2}$	V_{i2}	...	T_{orig}	...	T_{new}
		V_{i3}	T_{new}
		V_{new}	$T_{orig} \quad T_{new}$
15	edge	V_{i1}	T_{new}
	$V_{i2}-V_{i3}$	V_{i2}	
		V_{i3}	...	T_{orig}	...	T_{new}
		V_{new}	$T_{orig} \quad T_{new}$
	edge	V_{i1}	...	T_{orig}	...	T_{new}
	$V_{i3}-V_{i1}$	V_{i2}	T_{new}
		V_{i3}	
		V_{new}	$T_{orig} \quad T_{new}$

The last step is to update the edge-neighbors table in correspondence of the three vertices of the original triangle V_{i1} , V_{i2} and V_{i3} as well as the vertex projecting in the middle of the edge V_{new} , using the algorithm described above in equations (6) and (7). In the case of the present example, the edge-neighbors table is updated as follows:

25	<i>Triangle</i>	T_{i1}	T_{i2}	T_{i3}	(18)
	T_0	T_8	T_{1a}	T_{12}	
	T_{1a}	T_{1b}	T_0	T_4	
	T_{1b}	T_2	T_{12}	T_{1a}	
	

The geometry is now manifold as shown in Figure 9.

An efficient closest-vertex search is utilized in accordance with the present invention. If the entire geometry is searched, the number of calculations required to eliminate duplicate vertices and split triangles in order to obtain a connected, closed manifold is a function of the square of the number of vertices and shown by the following equation:

$$\frac{a}{2} \cdot n_e \cdot n_v = \frac{a}{2} \cdot \frac{n_e}{n_v} \cdot n_v^2 = \frac{a}{2} \cdot \frac{n_{e/v}}{2} \cdot n_v^2 = \frac{a}{2} \cdot \frac{3}{2} \cdot \frac{n_{t/v}}{2} \cdot n_v^2 \quad (19)$$

10

where n_e is the number of edges, n_v is the number of vertices, $\frac{n_{e/v}}{2}$ is the edge/vertex ratio, $\frac{n_{t/v}}{2} = \frac{2n_{e/v}}{3 \cdot 2}$ is the

triangle/vertex ratio, and a is the percentage of edges that are not connected and require some action. Since a typical tessellated model of a single vehicle component usually consists of hundreds of thousands of triangles, the number of computations quickly grows and becomes unmanageable when dealing with complex assemblies. Different solutions are available. Most of these are based on the same philosophy where all of the elements of the model are assigned to some bounding volumes of simple geometry. In order to reduce the number of computations from a linear to a logarithmic dimension, the hierarchy of bounding volumes is often used. Some implementations subdivide the space in spherical-containers, while others make use of variable-side bounding boxes.

25

With the present invention, the space is decomposed using an OctTree structure. This is a data-

structure, similar to a voxel map, and is in current use in computer-graphics. An example illustrates its concept. If the parent node of the OctTree is a box enclosing the entire workspace, vertices are assigned to it. As soon as there are more than a constant, assigned number of vertices in the parent node, for example 4, the box is split into a set of 8 identical smaller boxes, where the intersection is the empty set and the union is the original box. The elements previously assigned to the original box are then reassigned to the smaller containers. This is shown in Figure 10. As the sorting continues and new vertices are assigned to the proper boxes, the sub-box that is filled is once more subdivided into eight smaller volumes and so on. This is shown in Figure 11.

The data structure is bi-directional. Each node has a pointer linked to either a list of vertices or a list of sub-boxes. On the other hand, each vertex has embedded in its coordinate the address of the box containing it. Since the boxes are always split and each side is dissected into two equal segments, it is sufficient to find the address of the box to normalize the coordinates by the size of the workspace and then multiple the result by 2^n , where n is the maximum number of layers, and round off to the nearest integer. For example, given the point shown in Figure 12, the address in an $n=4$ layers OctTree is as follows:

$$\text{int}\left(\frac{x - x_{\min}}{x_{\max} - x_{\min}} \cdot 2^4\right), \text{int}\left(\frac{y - y_{\min}}{y_{\max} - y_{\min}} \cdot 2^4\right) \Rightarrow 0011, 0001 \quad (20)$$

These indexes can be used to find the containing box. If the parent node points to a list of

vertices, then the search is completed. Otherwise, the Most Significant Bits (MSB) defines the address of the sub-box which in this case is box 0,0. If this box had been subdivided, the child container is found by
5 shifting the indexes to the left and using the MSBs once more. In the particular example shown above, the procedure ends after the indexes had been shifted three times. The sequence of boxes is then as follows: 00, 00, 10, 11.

10 Most vertices can be eliminated by looking only at those inside boxes whose intersections with the given shape is not null. To identify these boxes, one possibility is to find the smallest box in the OctTree index space enclosing the edge plus a neighborhood
15 region function of epsilon. To do so, it is first necessary to map the edge equation from Cartesian to the OctTree index space. The edge is defined as the parameter α as:

$$(x_0, y_0, z_0) + \alpha \cdot (\Delta x, \Delta y, \Delta z), \text{ with } \|\Delta x, \Delta y, \Delta z\|_2 = 1$$

20 and $0 \leq \alpha \leq \alpha_{\max}$ and it starts in $P_0 = (x_0, y_0, z_0)$ (21)
and ends in $P_1 = (x_0, y_0, z_0) + \alpha_{\max} (\Delta x, \Delta y, \Delta z)$.

Assuming all positive $\Delta x, \Delta y, \Delta z$, the maximum and minimum indexes of a box, aligned with the system axis and enclosing the edges are:

25

$$\bar{i}_{\min} = \left\{ \text{int} \left(\frac{P_{0,x} - x_{\min}}{x_{\max} - x_{\min}} \cdot 2^n \right), \text{int} \left(\frac{P_{0,y} - y_{\min}}{y_{\max} - y_{\min}} \cdot 2^n \right), \text{int} \left(\frac{P_{0,z} - z_{\min}}{z_{\max} - z_{\min}} \cdot 2^n \right) \right\}$$

$$\bar{i}_{\max} = \left\{ \text{int} \left(\frac{P_{1,x} - x_{\min}}{x_{\max} - x_{\min}} \cdot 2^n \right), \text{int} \left(\frac{P_{1,y} - y_{\min}}{y_{\max} - y_{\min}} \cdot 2^n \right), \text{int} \left(\frac{P_{1,z} - z_{\min}}{z_{\max} - z_{\min}} \cdot 2^n \right) \right\}$$

(22)

A more efficient alternative is to only check the boxes that are in the close neighborhood of the edge, as shown in Figure 15. The equation of the edge in Cartesian space, which is

$$P(a) = (x_0, y_0, z_0) + \alpha \cdot (\Delta x, \Delta y, \Delta z) \quad (28)$$

with $\|\Delta x, \Delta y, \Delta z\|_2 = 1$ and $0 \leq \alpha \leq \alpha_{\max}$

becomes the OctTree index space

$$\bar{i}(a) = 2^n \cdot \left[\left(\frac{x_0 - x_{\min}}{x_{\max} - x_{\min}}, \frac{y_0 - y_{\min}}{y_{\max} - y_{\min}}, \frac{z_0 - z_{\min}}{z_{\max} - z_{\min}} \right) + \alpha \cdot \left(\frac{\Delta x}{z_{\max} - z_{\min}}, \frac{\Delta y}{z_{\max} - z_{\min}}, \frac{\Delta z}{z_{\max} - z_{\min}} \right) \right] \quad (29)$$

Using this equation, it is now possible to traverse the tree and for each box to determine if it contains a portion of the edge. Even if the technique requires additional computations to determine the list of boxes to be included in the search, it culls some of the boxes that would otherwise have been selected and as a consequence reduces the number of vertices whose distance from the target needs to be evaluated. On average, the overall number of calculations is less than in the previous implementation. Since OctTree are three-dimensional binary trees, the searching algorithm in accordance with the present invention has a logarithmic, base 2, complexity.

While the invention has been described in connection with one or more embodiments, it is to be understood that the specific mechanisms and techniques which have been described are merely illustrative of the principles of the invention. Numerous modifications may be made to the methods and apparatus

described without departing from the spirit and scope of the invention as defined by the appended claims.

What Is Claimed Is:

1. A method for reconstructing topological information for a mesh, said mesh comprising a polygonal soup of triangles with sides and vertices,
5 said method comprising the steps of:
building vertex and edge connectivity data;
finding duplicates of vertices;
removing said duplicates of vertices; and
realigning strips of triangles without common
10 vertices.
2. The method as set forth in claim 1 wherein said step of building vertex and edge connectivity data comprises the steps of:
generating a representative index;
15 creating a vertex-neighbor table; and
building an edge-neighbor table.
3. The method as recited in claim 2 wherein said step of generating a representative index comprises eliminating at least one duplication of
20 vertices.
4. The method as recited in claim 2 wherein said step of removing duplicate vertices comprises:
searching for unconnected sides of triangles;
searching for duplicates of the vertices at
25 the ends of said unconnected sides;
replacing all duplicate vertices with original vertices;
adding triangles connected to the duplicate vertices to said original vertices; and

rebuilding said edge-neighbor table for all triangles connected to said original vertices.

5 5. The method as set forth in claim 4 wherein said step of adding triangles comprises splitting the triangles into new smaller triangles.

6. The method as set forth in claim 4 wherein said step of searching for duplicates comprises searching in said vertex-neighbor table for the closest vertex.

10 7. The method as set forth in claim 6 wherein said step of searching for the closest vertex comprises using an OctTree structure.

15 8. The method as set forth in claim 6 wherein said step of searching for the closest vertex comprises using a log2-complexity search method.

9. The method as set forth in claim 8 wherein said log2-complexity search method comprises using an OctTree structure.

Abstract Of The Disclosure

A method for automatically reconstructing topographical information for a given mesh, altering the mesh by introducing, deleting, or splitting existing polygons when needed. An OctTree space decomposition is used to achieve a log2-complexity search method to find the closest vertex in the polygonal soup to a given point in space. Linear complexities are used to find triangles connected to a given vertex and all triangles connected to a given triangle. The triangles are split to enforce conductivity.

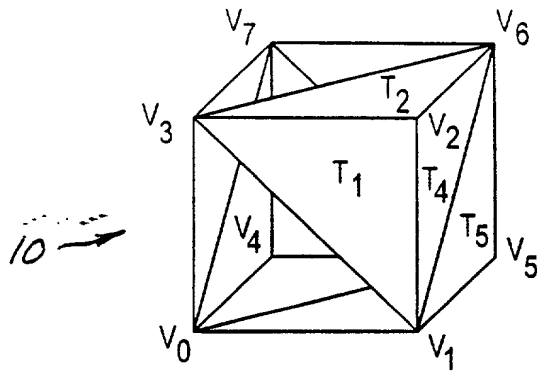


FIG. 1

solid CUBE

facet

outer loop

vertex -1 -1 +1

vertex +1 -1 +1

vertex -1 +1 +1

endloop

endfacet

facet

outerloop

vertex +1 +1 +1

vertex -1 +1 +1

vertex +1 -1 +1

endloop

endfacet

facet

outer loop

vertex +1 +1 +1

vertex +1 +1 -1

vertex -1 +1 +1

endloop

endfacet

.....

.....

endsolid CUBE

Triangle	V _{i1}	V _{i2}	V _{i3}
T ₀	V ₀	V ₁	V ₃
T ₁	V ₂	V ₃	V ₁
T ₂	V ₂	V ₆	V ₃
T ₃	V ₇	V ₃	V ₆
T ₄	V ₂	V ₁	V ₆
T ₅	V ₅	V ₆	V ₁
T ₆	V ₄	V ₇	V ₅
T ₇	V ₆	V ₅	V ₇
T ₈	V ₁	V ₀	V ₅
T ₉	V ₄	V ₅	V ₀
T ₁₀	V ₃	V ₇	V ₀
T ₁₁	V ₄	V ₀	V ₇

Vertex	X	Y	Z
V ₀	-1	-1	+1
V ₁	+1	-1	+1
V ₂	+1	+1	+1
V ₃	-1	+1	+1
V ₄	-1	-1	-1
V ₅	+1	-1	-1
V ₆	+1	+1	-1
V ₇	-1	+1	-1

FIG. 2

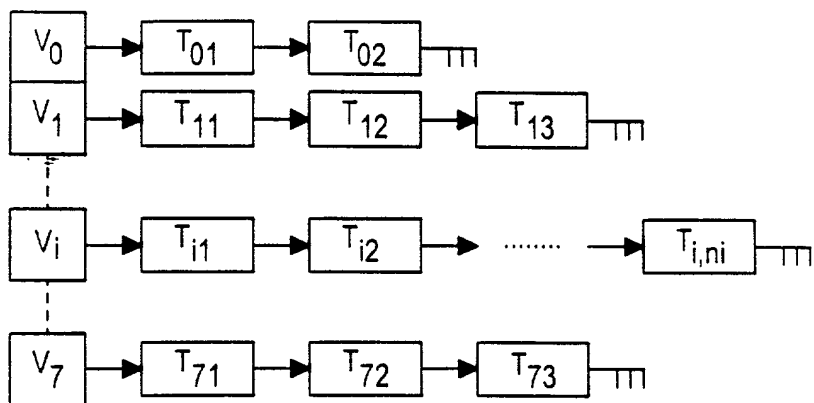


FIG. 3

Vertex	T_{i1}	T_{i2}	Vertex	T_{i1}	T_{i2}	Vertex	T_{i1}	T_{i2}
V_0	T_0		V_0	T_0		V_0	T_0	T_8	T_9	T_{10}	T_{11}
V_1	T_0		V_1	T_0	T_1	V_1	T_0	T_1	T_4	T_5	T_8
V_2			V_2	T_1		V_2	T_1	T_2	T_4		
V_3	T_0		V_3	T_0	T_1	V_3	T_0	T_1	T_2	T_3	T_{10}
V_4			V_4			V_4	T_6	T_9	T_{11}		
V_5			V_5			V_5	T_5	T_6	T_7	T_8	T_9
V_6			V_6			V_6	T_2	T_3	T_4	T_5	T_7
V_7			V_7			V_7	T_3	T_6	T_7	T_{10}	T_{11}

A
B
C

FIG. 4

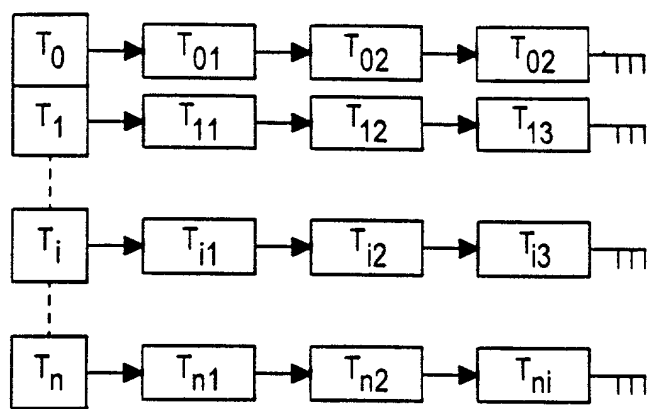


FIG. 5

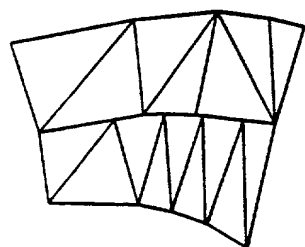


FIG. 6

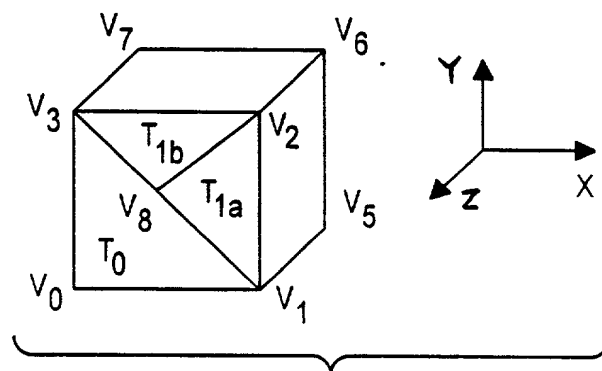


FIG. 7

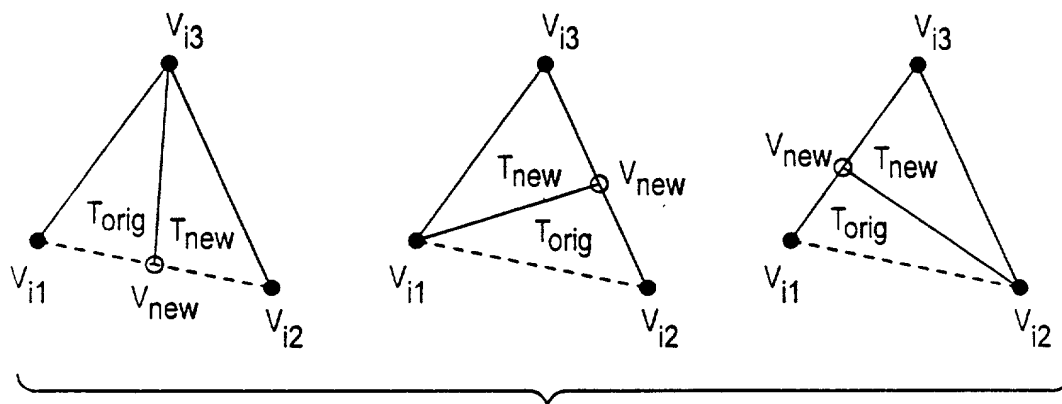


FIG. 8

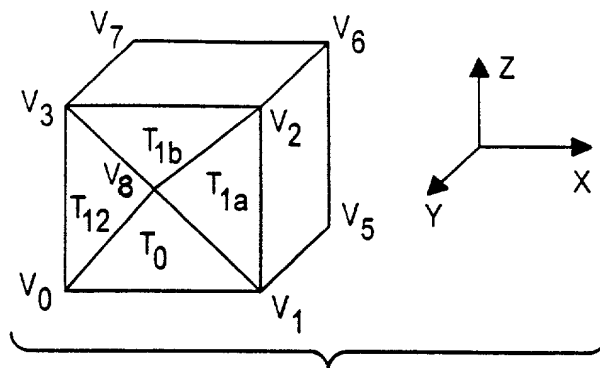


FIG. 9

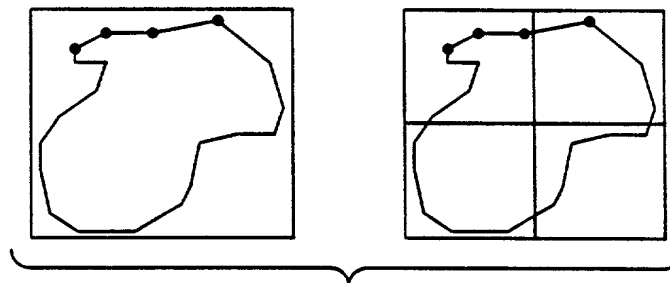


FIG. 10

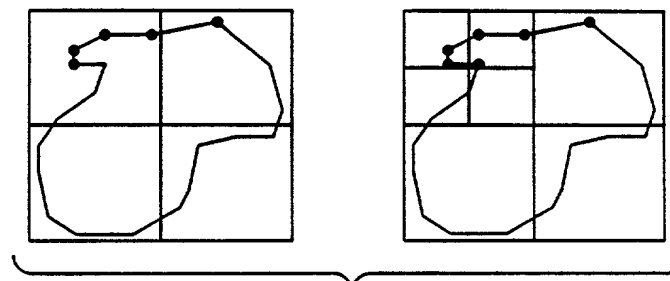


FIG. 11

	0000	0010	0100	1000
0000	0,0	0,1	0,1	0,1
0010				
0100	●	1,1		
	1,0	1,1		
1000	1,0			1,1

FIG. 12

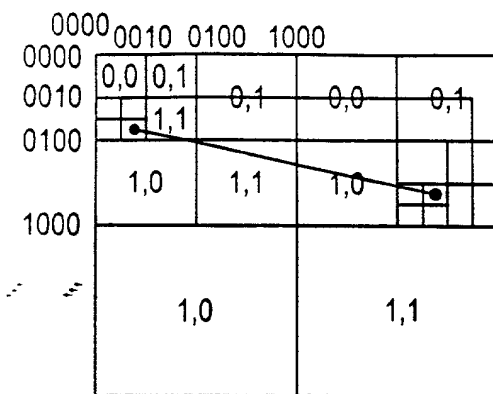


FIG. 13

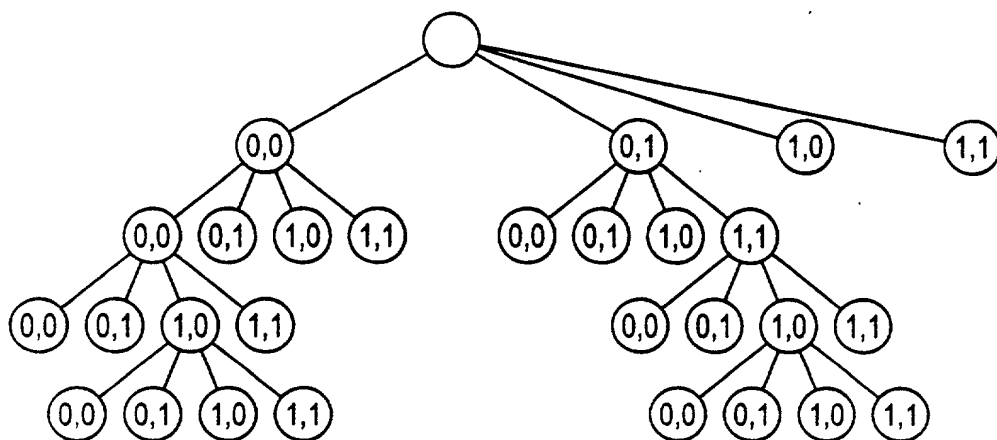


FIG. 14

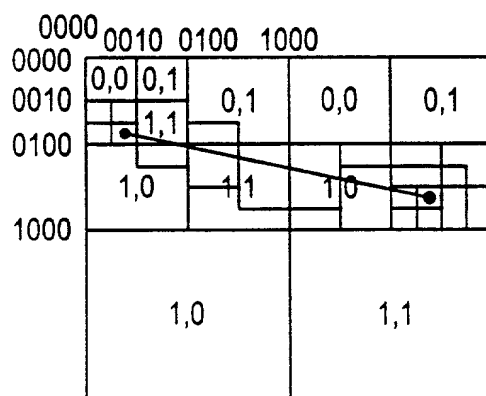


FIG. 15

DECLARATION AND POWER OF ATTORNEY - ORIGINAL APPLICATION

Attorney's Docket No.
200-0032

As a below named inventor, I hereby declare:
My residence, post office address and citizenship are as stated below next to my name;

I verily believe I am the original, first and sole inventor or an original, first and joint inventor of the subject matter that is claimed and for which a patent is sought on the invention entitled

METHOD FOR RECONSTRUCTING THE TOPOGRAPHICAL INFORMATION OF A POLYGONAL SOUP

the specification of which is attached hereto.

I have reviewed and understand the contents of the specification identified above, including the claims.

I acknowledge my duty to disclose information of which I am aware that is material to the examination of this application in accordance with Section 1.56(a), Title 37 of the Code of Federal Regulations; and

as to application for patents or inventor's certificate on the invention filed in any country foreign to the United States of America, prior to this application by me or my legal representatives or assigns,

☒ no such applications have been filed, or

☐ such applications have been filed as follows

COUNTRY	APPLICATION NO.	DATE OF FILING (day, month, year)	DATE OF ISSUE (day, month, year)	PRIORITY CLAIMED UNDER 35 USC 119

I hereby claim the benefit under 35 U.S.C. § 120 of any United States application(s) or § 365(c) of any PCT International application designating the United States, listed below and, insofar as the subject matter of each of the claims of this application is not disclosed in the prior United States or PCT International application in the manner provided by the first paragraph of 35 U.S.C. § 112, I acknowledge the duty to disclose information which is material to patentability as defined in 37 CFR § 1.56 which became available between the filing date of the prior application and the national or PCT International filing date of this application.

(Application Number) (Filing Date) (Status - patented, pending, abandoned)

(Application Number) (Filing Date) (Status - patented, pending, abandoned)

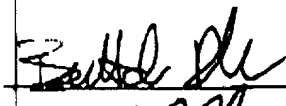
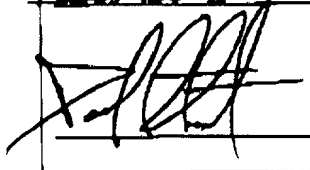
POWER OF ATTORNEY: As a named inventor, I hereby appoint the following attorney(s) and/or agent(s) to prosecute this application and transact all business in the United States Patent and Trademark Office connected therewith and to act on my behalf before the competent International Authorities in connection with any and all international applications filed by me.
(List name and registration number)

John A. Artz - 25,824
Damian Porcari - 31,461
Roger L. May - 26,406

Address all correspondence and telephone calls to:

John A. Artz
Artz & Artz PLC
28333 Telegraph Road, Suite 250
Southfield, MI 48034 Phone: 248 223-9500

I hereby declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true; and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under Section 1001 of Title 18 of the United States Code, and that such willful false statements may jeopardize the validity of the application or any patent issuing thereon.

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Attorney Docket No: 200-0032

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